### CSE 152: Computer Vision Hao Su

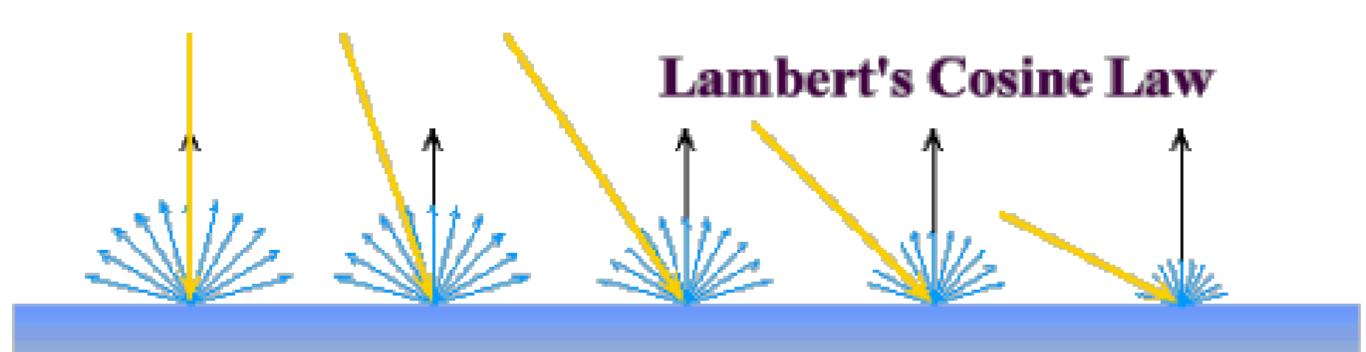
#### **Filters and Features**



### Diffuse reflection: Lambert's cosine law

Intensity does not depend on viewer angle.

- Amount of reflected light proportional to  $cos(\theta)$
- Visible solid angle also proportional to  $\cos(\theta)$

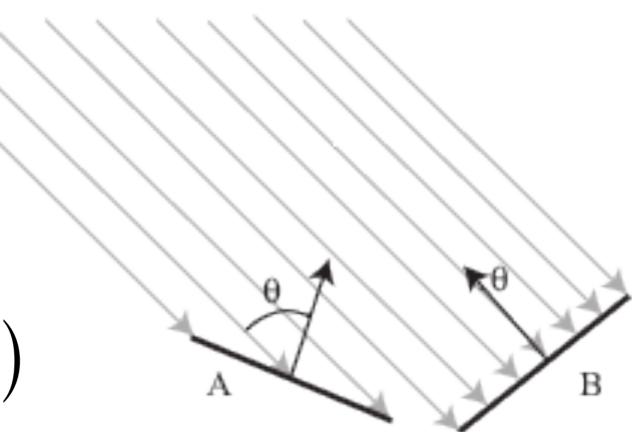


### Intensity and Surface Orientation

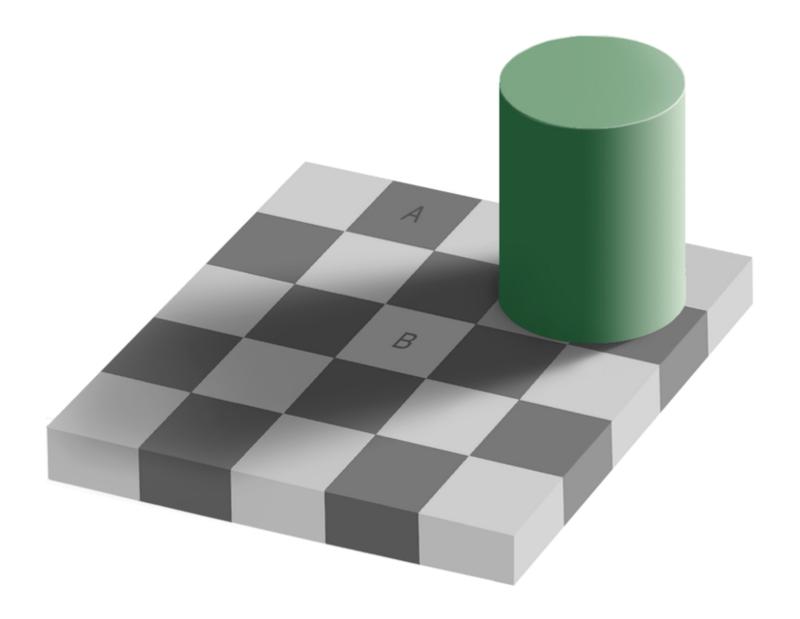
Intensity depends on illumination angle because less light comes in at oblique angles.

- $\rho = albedo$
- S = directional source
- *N* = surface normal
- I = reflected intensity

 $I(x) = \rho(x) \big( \boldsymbol{S} \cdot \boldsymbol{N}(x) \big)$ 

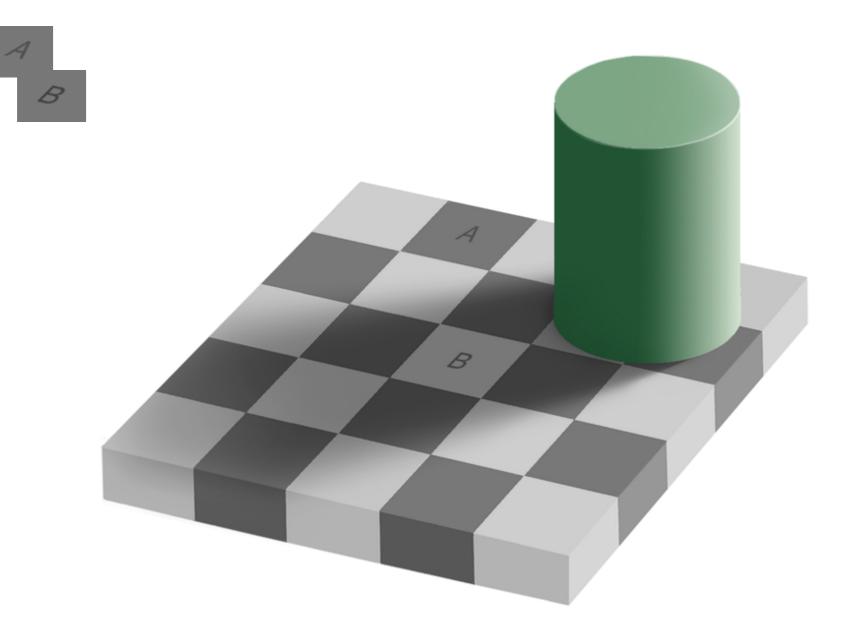


### Perception of Intensity



from Ted Adelso

### Perception of Intensity



from Ted Adelso

#### Darkness = Large Difference in Neighboring Pixels



### Why should we care?



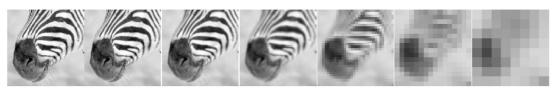
Input

#### Smoothing

#### Sharpening

https://en.wikipedia.org/wiki/Albert\_Einstein\_in\_popular\_culture#/media/ File:Einstein\_tongue.jpg

### Why should we care?



512 256 128 64 32 16 8



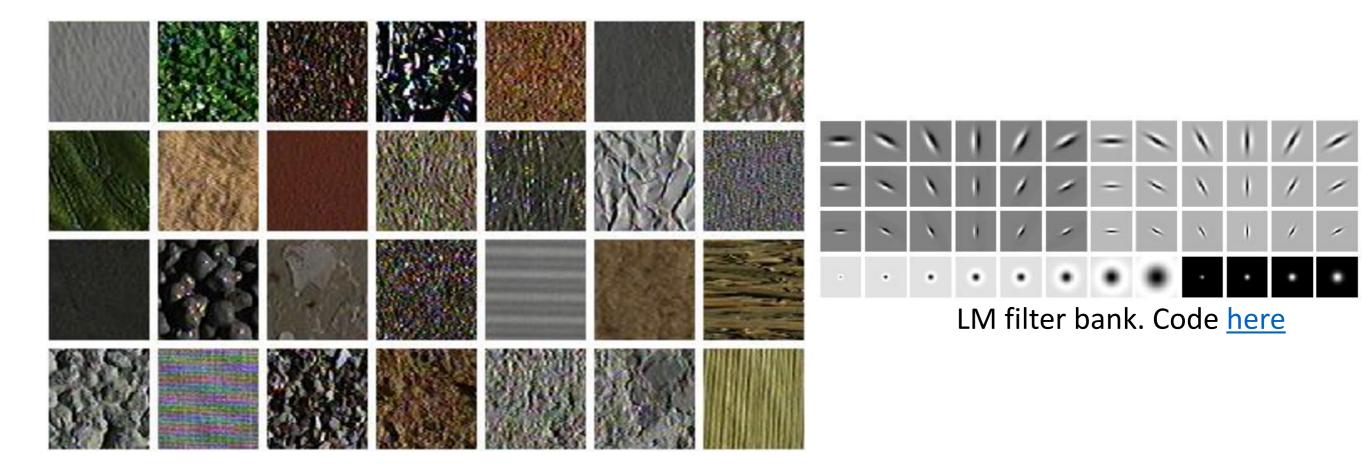


#### Image interpolation/resampling Source: N Shavely

Image Pyramid

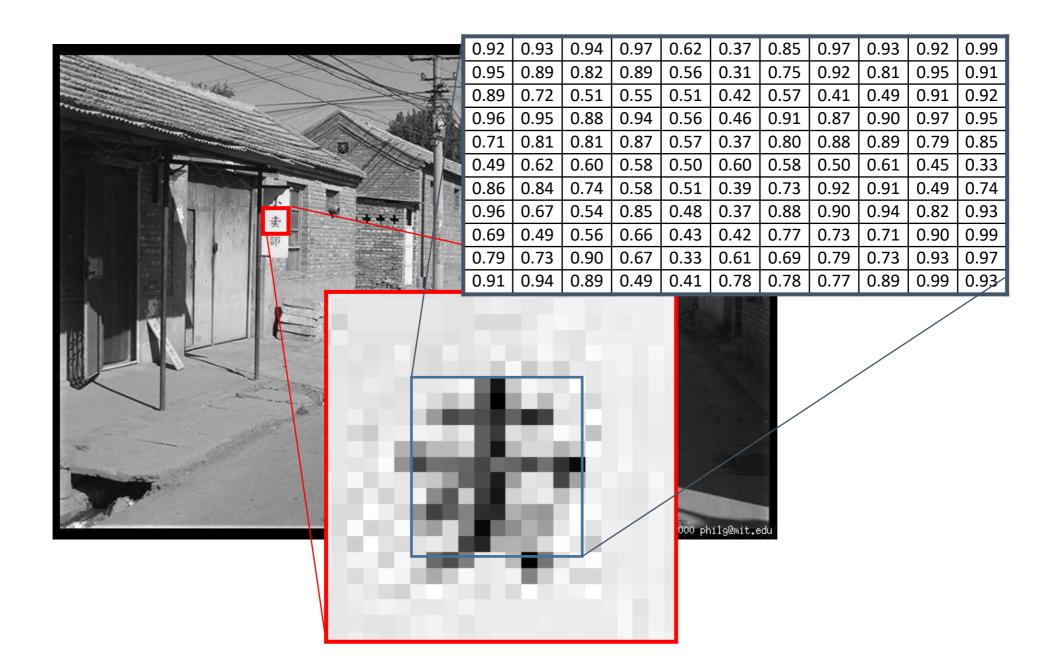
Source: D Forsyth

## Why should we care?



Representing textures with filter banks

### The raster image (pixel matrix)



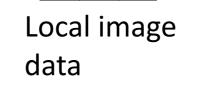
- For each pixel, compute function of local neighborhood and output a new value
  - Same function applied at each position
  - Output and input image are typically the same size



- Linear filtering
  - function is a weighted sum/difference of pixel values



- Enhance images
  - Denoise, smooth, increase contrast, etc.
- Extract information from images
  - Texture, edges, distinctive points, etc.
- Detect patterns
  - Template matching



5

6

1

3

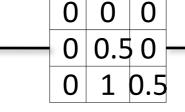
1

8

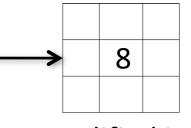
10

4

1



kernel



Modified image data

## **Question: Noise reduction**

• Given a camera and a still scene, how can you reduce noise?

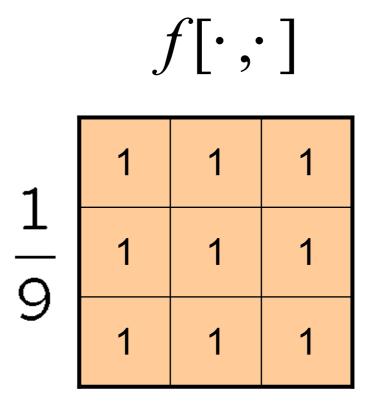


#### Take lots of images and average them! What's the next best thing?

### First attempt at a solution

- Let's replace each pixel with an average of all the values in its neighborhood
- Assumptions:
  - Expect pixels to be like their neighbors
  - Expect noise processes to be independent from pixel to pixel

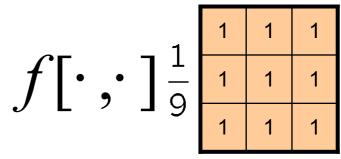
#### Example: box filter



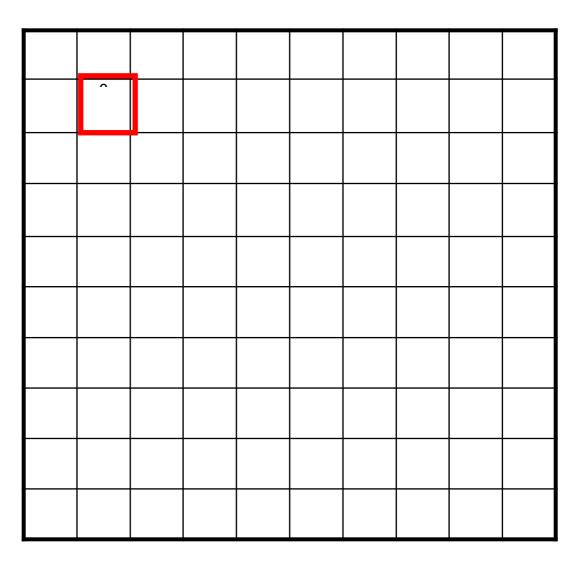
Slide credit: David Lowe (UBC)



0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



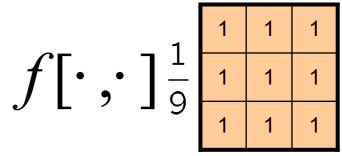
h[.,.]



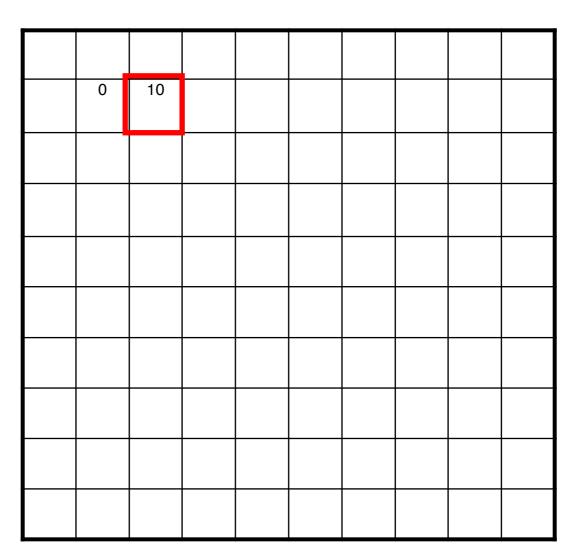
 $h[m,n] = \sum_{k,l} f[k,l] I[m+k,n+l]$ 



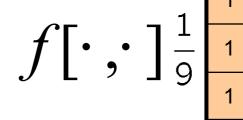
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



h[.,.]



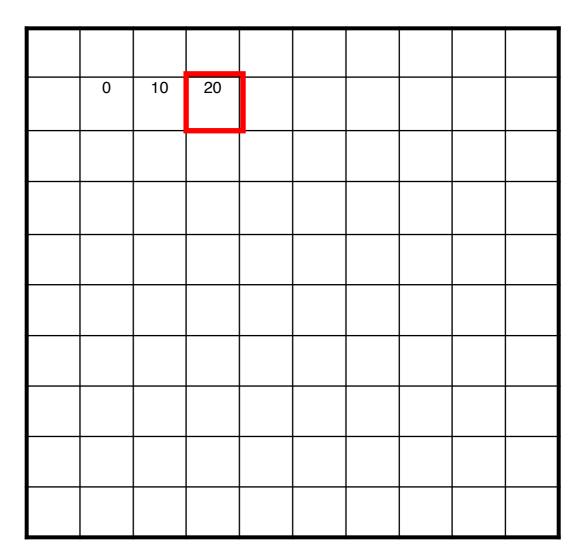
 $h[m,n] = \sum_{k,l} f[k,l] I[m+k,n+l]$ 



1	1	1	1
- 	1	1	1
9	1	1	1

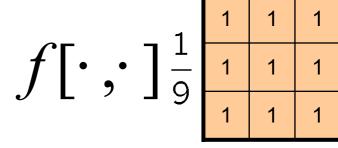
*I*[.,.]

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



h[.,.]

 $h[m,n] = \sum_{k,l} f[k,l] I[m+k,n+l]$ 



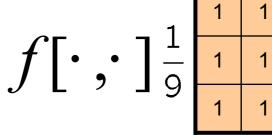
*I*[.,.]

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

0	10	20	30			

h[.,.]

 $h[m,n] = \sum_{k,l} f[k,l] I[m+k,n+l]$ 



1	1	1	1
-  T	1	1	1
9	1	1	1

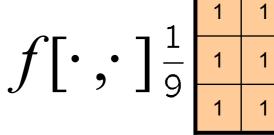
*I*|.,|

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

0	10	20	30	30		

h[.,.]

 $h[m,n] = \sum_{k=1}^{\infty} f[k,l] I[m+k,n+l]$ 



1	1	1	1
	1	1	1
9	1	1	1

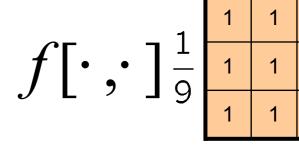
*I*|.,|

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	U	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

0	10	20	30	30		
			?			

h[.,.]

 $h[m,n] = \sum_{k=1}^{\infty} f[k,l] I[m+k,n+l]$ 



1

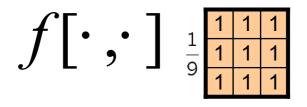
*I*[.,.]

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

0	10	20	30	30			
					?		
			50				

h[.,.]

 $h[m,n] = \sum_{k,l} f[k,l] I[m+k,n+l]$ 



*I*[.,.]

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

h[.,.]

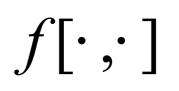
0	10	20	30	30	30	20	10	
0	20	40	60	60	60	40	20	
0	30	60	90	90	90	60	30	
0	30	50	80	80	90	60	30	
0	30	50	80	80	90	60	30	
0	20	30	50	50	60	40	20	
10	20	30	30	30	30	20	10	
10	10	10	0	0	0	0	0	

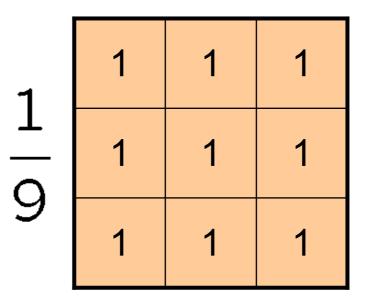
 $h[m,n] = \sum_{k,l} f[k,l] I[m+k,n+l]$ 

#### **Box Filter**

#### What does it do?

- Replaces each pixel with an average of its neighborhood
- Achieve smoothing effect (remove sharp features)





### Smoothing with box filter





# Properties of smoothing filters

### <u>Smoothing</u>

- Values positive
- Sum to 1  $\rightarrow$  constant regions same as input
- Amount of smoothing proportional to mask size
- Remove "high-frequency" components; "low-pass" filter

# **Correlation filtering**

Say the averaging window size is 2k+1 x 2k+1:

$$G[i,j] = \frac{1}{(2k+1)^2} \sum_{u=-k}^{k} \sum_{v=-k}^{k} F[i+u,j+v]$$

AttributeLoop over all pixels inuniform weightneighborhood around imageto each pixelpixel F[i,j]

Now generalize to allow different weights depending on neighboring pixel's relative position:

$$G[i, j] = \sum_{u=-k}^{k} \sum_{v=-k}^{k} H[u, v] F[i + u, j + v]$$

$$K_{i} = \sum_{u=-k}^{k} \sum_{v=-k}^{k} H[u, v] F[i + u, j + v]$$

$$K_{i} = \sum_{u=-k}^{k} F[i + u, j + v]$$

## **Correlation filtering**

$$G[i,j] = \sum_{u=-k}^{k} \sum_{v=-k}^{k} H[u,v]F[i+u,j+v]$$

This is called cross-correlation, denoted  $G = H \otimes F$ 

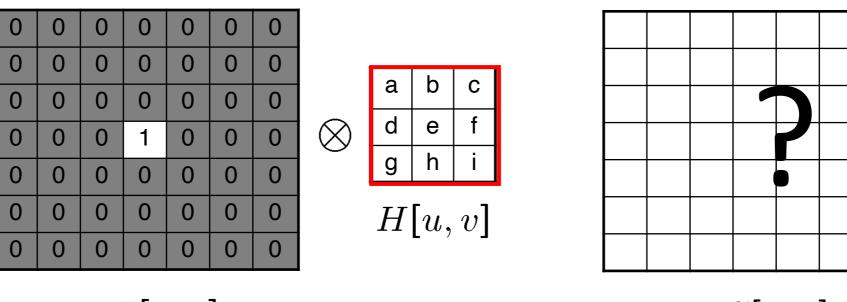
Filtering an image: replace each pixel with a linear combination of its neighbors.

The filter "kernel" or "mask" H[u,v] is the prescription for the weights in the linear combination.

Slide credit: Kristen Grauman

# Filtering an impulse signal

What is the result of filtering the impulse signal (image) *F* with the arbitrary kernel *H*?



F[x, y]

G[x, y]

# Convolution

- Convolution:
  - Flip the filter in both dimensions (bottom to top, right to left)
  - Then apply cross-correlation

### **Convolution vs. correlation**

Convolution  

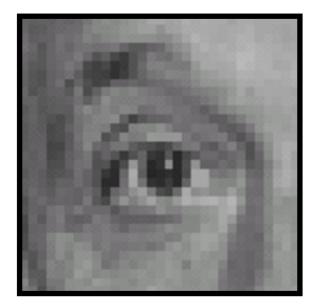
$$G[i,j] = \sum_{u=-k}^{k} \sum_{v=-k}^{k} H[u,v]F[i-u,j-v] \qquad G=conv2(H,F);$$

$$G = H \star F$$

#### **Cross-correlation**

$$G[i,j] = \sum_{u=-k}^{k} \sum_{v=-k}^{k} H[u,v]F[i+u,j+v] \qquad \qquad \text{G=filter2(H,F); Or} \\ G=\text{imfilter(F,H);}$$

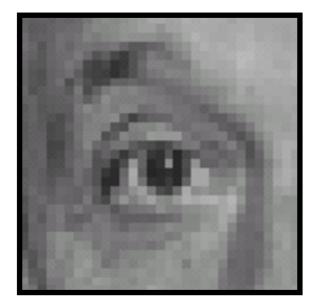
 $G = H \otimes F$ For a Gaussian or box filter, how will the outputs differ? If the input is an impulse signal, how will the outputs differ?



000010000

?

Original

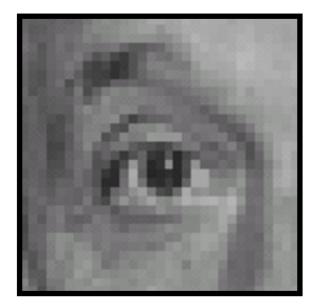


Original

0	0	0
0	1	0
0	0	0



Filtered (no change)

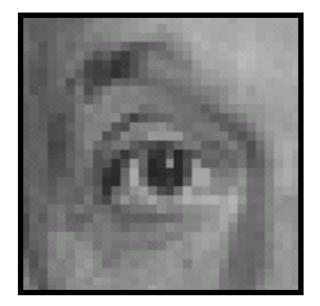


000001000

?

Original

Source: D. Lowe



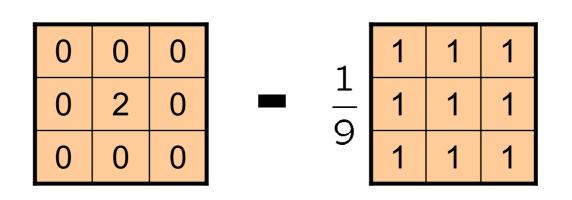
Original

0	0	0
0	0	1
0	0	0



Shifted left By 1 pixel



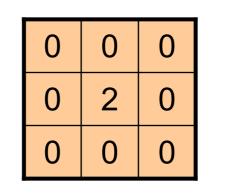


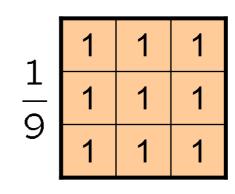
(Note that filter sums to 1)

Original

#### Practice with linear filters







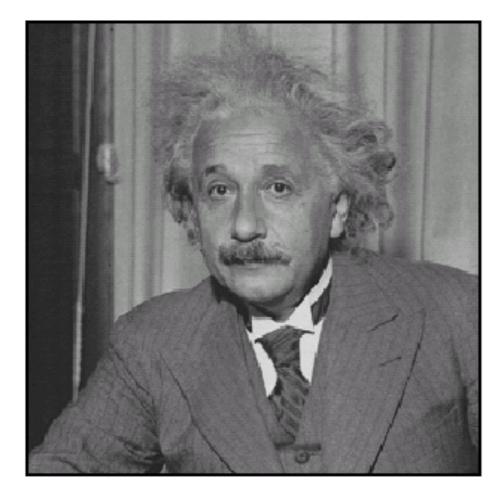


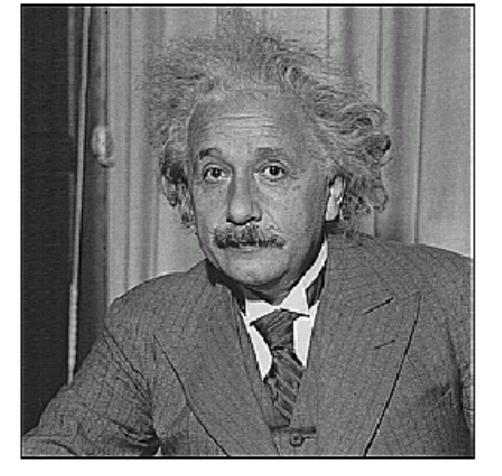
Original

#### **Sharpening filter**

- Accentuates differences with local average

## Sharpening

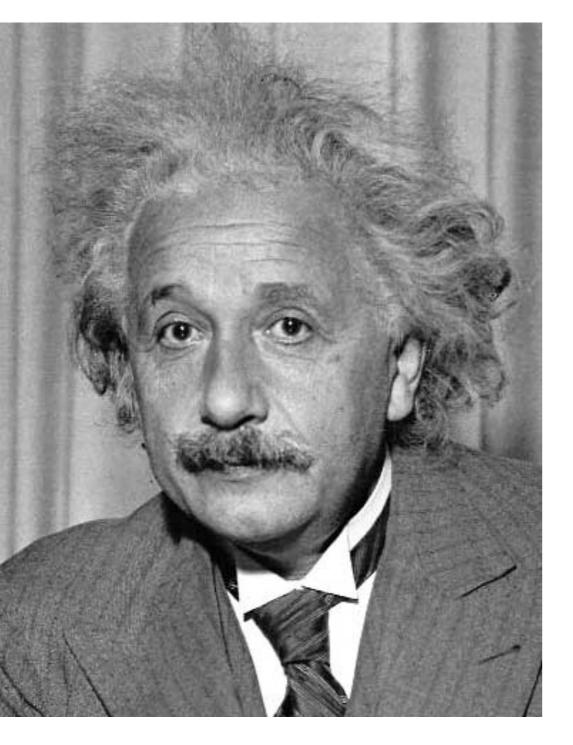




before

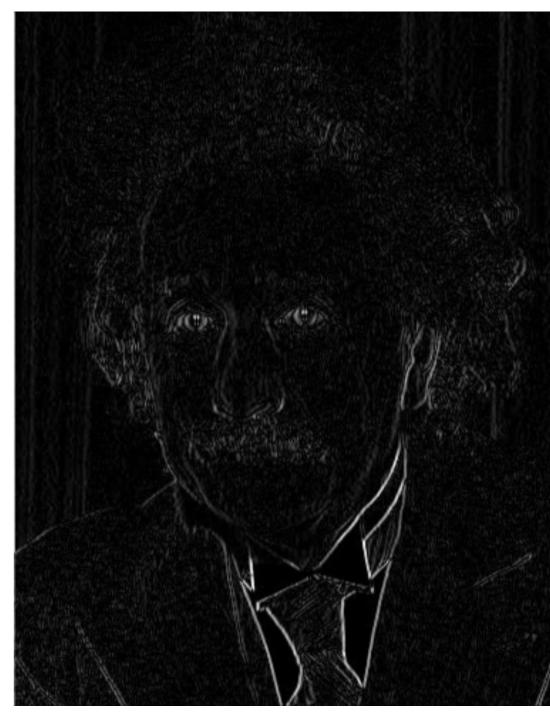
after

### Other filters



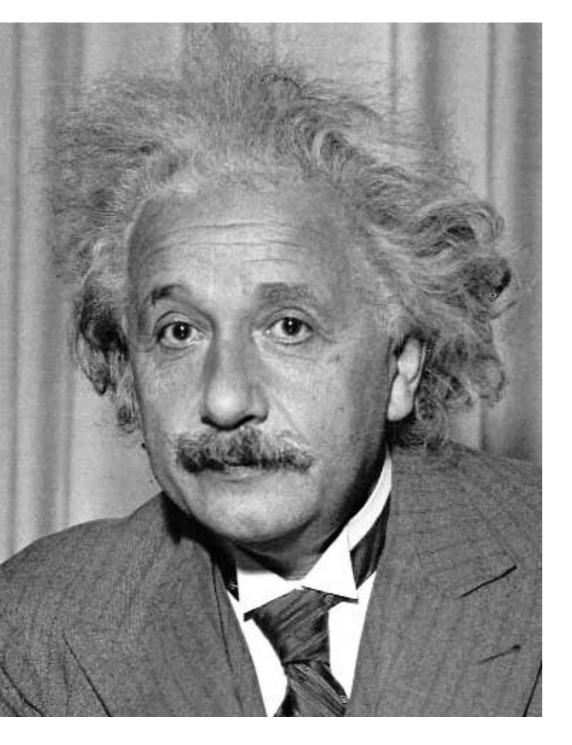
1	0	-1
2	0	-2
1	0	-1

Sobel



Vertical Edge (absolute value)

### Other filters



1	2	1
0	0	0
-1	-2	-1

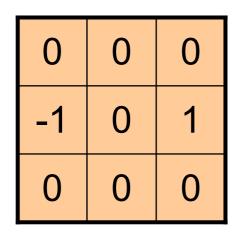
Sobel



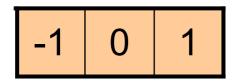
Horizontal Edge (absolute value)

### Basic gradient filters

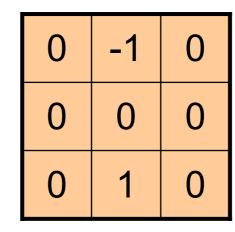
#### Horizontal Gradient



or



#### **Vertical Gradient**



-1 0 1

or

## Filtering vs. Convolution

2d filtering
 h=tf.nn.conv2d(f,g,...);

$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

• 2d convolution

$$h[m,n] = \sum_{k,l} g[k,l] f[m-k,n-l]$$

# Key properties of linear filters

#### Linearity:

filter( $f_1 + f_2$ ) = filter( $f_1$ ) + filter( $f_2$ )

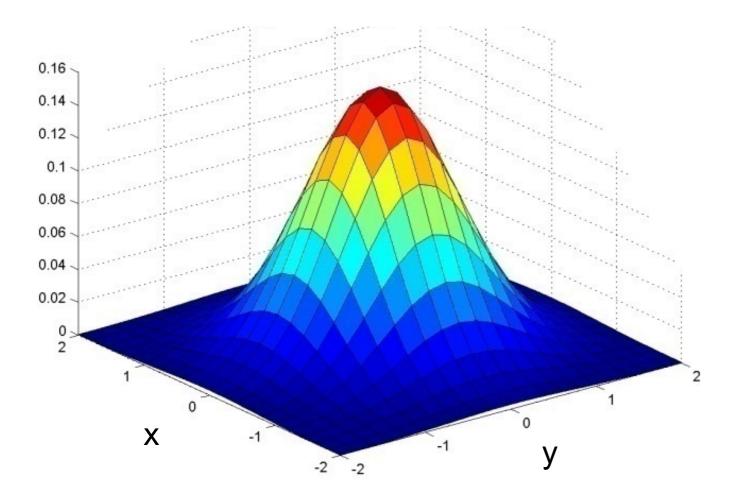
Shift invariance: same behavior regardless of pixel location
filter(shift(f)) = shift(filter(f))

Any linear, shift-invariant operator can be represented as a convolution

Source: S. Lazebnik

#### Important filter: Gaussian

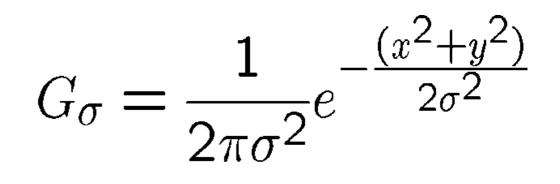
• Weight contributions of neighboring pixels by nearness



_		

			Х		
	0.003	0.013	0.022	0.013	0.003
	0.013	0.059	0.097	0.059	0.013
У	0.022	0.097	0.159	0.097	0.022
	0.013	0.059	0.097	0.059	0.013
	0.003	0.013	0.022	0.013	0.003
	L				

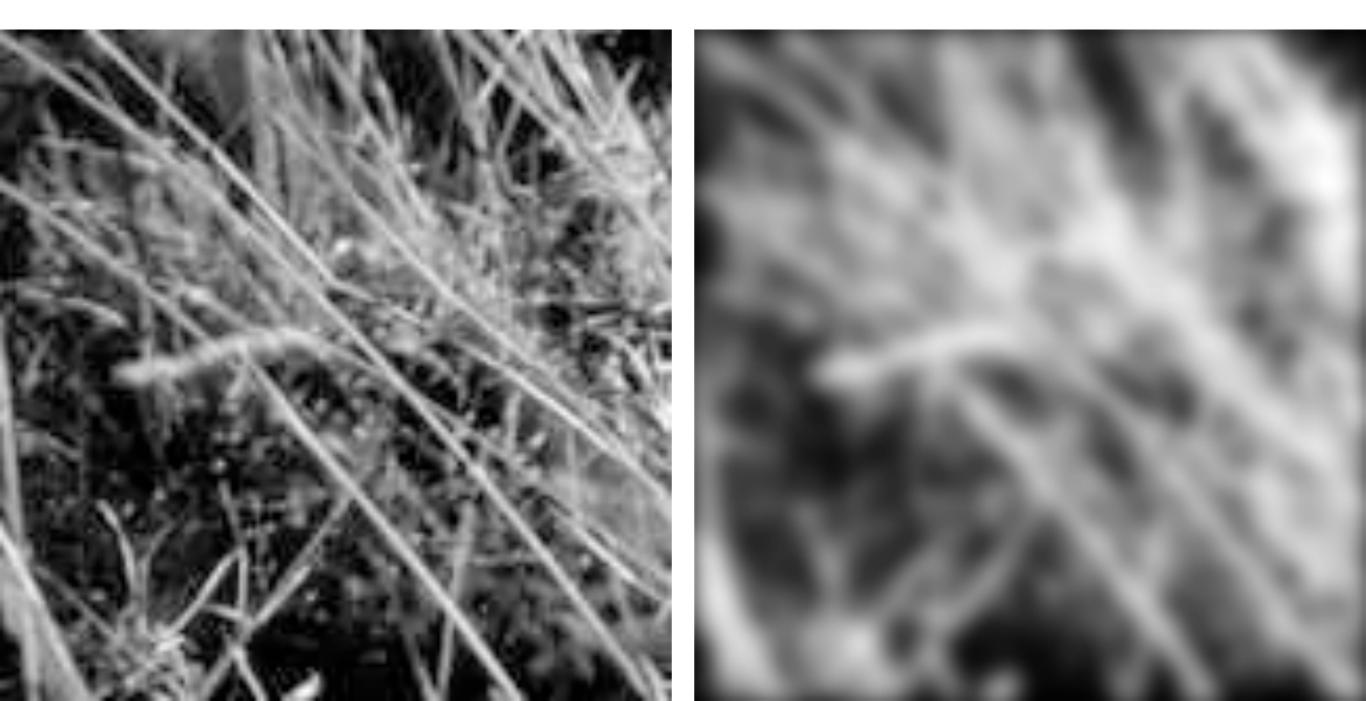
5 x 5,  $\sigma$  = 1



Slide credit: Christopher Rasmussen

### Smoothing with Gaussian filter



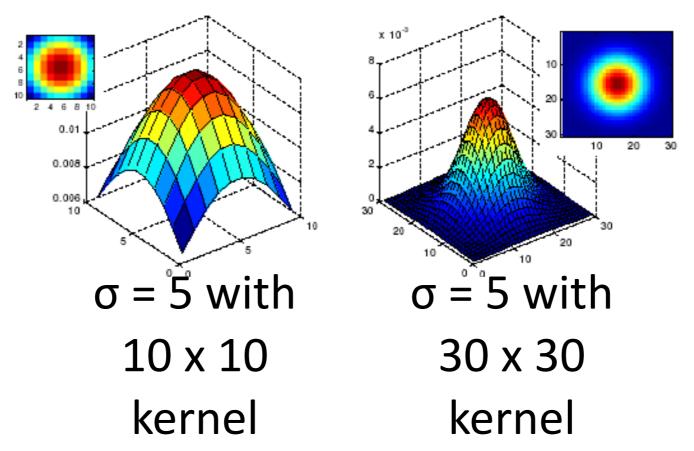


# Gaussian filters

- Remove "high-frequency" components from the image (low-pass filter)
  - Images become more smooth
- Convolution with self is another Gaussian
  - So can smooth with small-width kernel, repeat, and get same result as larger-width kernel would have
  - Convolving two times with Gaussian kernel of width  $\sigma$  is same as convolving once with kernel of width  $\,\sigma\sqrt{2}\,$

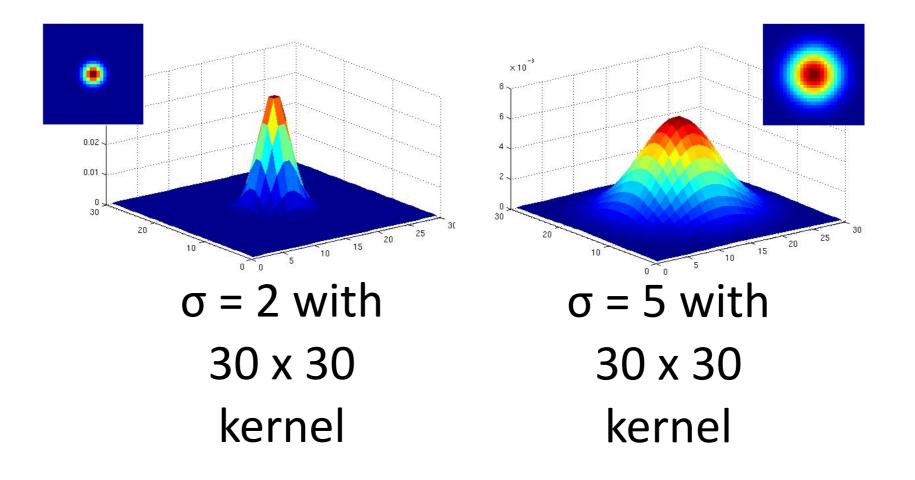
# Gaussian filters

- What parameters matter here?
- Size of kernel or mask
  - Note, Gaussian function has infinite support, but discrete filters use finite kernels



# Gaussian filters

- What parameters matter here?
- Variance of Gaussian: determines extent of smoothing



# Practical matters

- What about near the edge?
  - the filter window falls off the edge of the image
  - need to extrapolate
  - methods:
    - clip filter (black)
    - wrap around
    - copy edge
    - reflect across edge



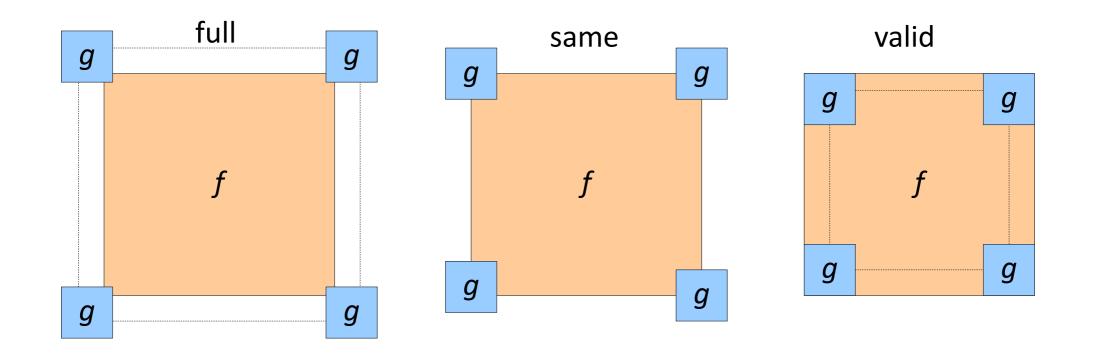
# **Practical matters**

#### • methods (MATLAB):

- clip filter (black):
- copy edge:
- reflect across edge:
- imfilter(f, g, 0)
- imfilter(f, g, 'replicate')
- imfilter(f, g, 'symmetric')

# **Practical matters**

- What is the size of the output?
- MATLAB: filter2(g, f, shape)
  - *shape* = 'full': output size is sum of sizes of f and g
  - *shape* = 'same': output size is same as f
  - shape = 'valid': output size is difference of sizes of f and g



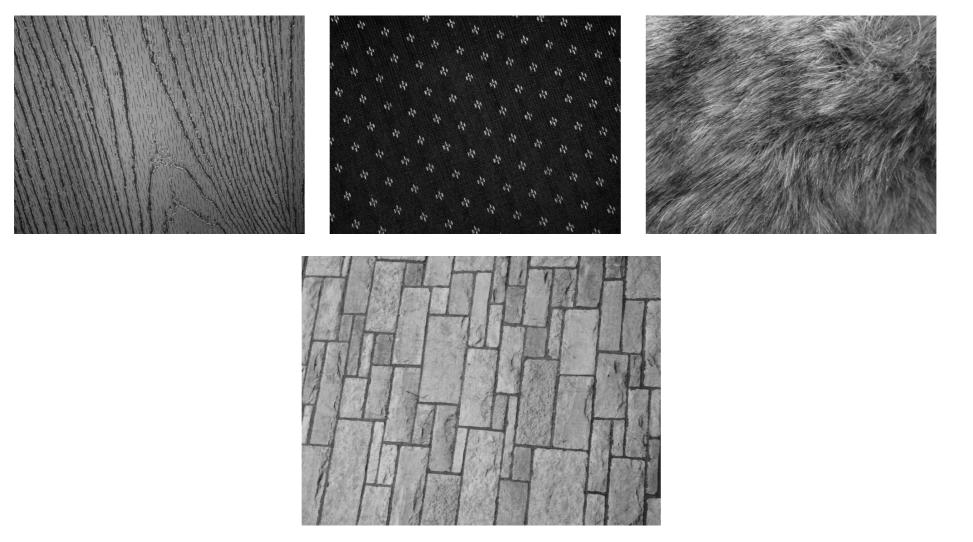
# 2-mins break

# **Application: Representing Texture**



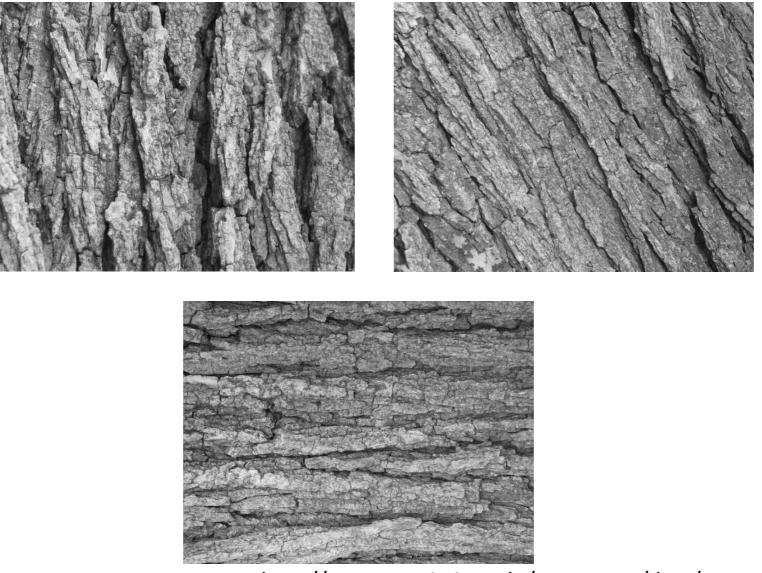
Source: Forsyth

## **Texture and Material**



http://www-cvr.ai.uiuc.edu/ponce\_grp/data/texture\_database/samples/

## **Texture and Orientation**



http://www-cvr.ai.uiuc.edu/ponce\_grp/data/texture\_database/samples/

### Texture and Scale



http://www-cvr.ai.uiuc.edu/ponce\_grp/data/texture\_database/samples/

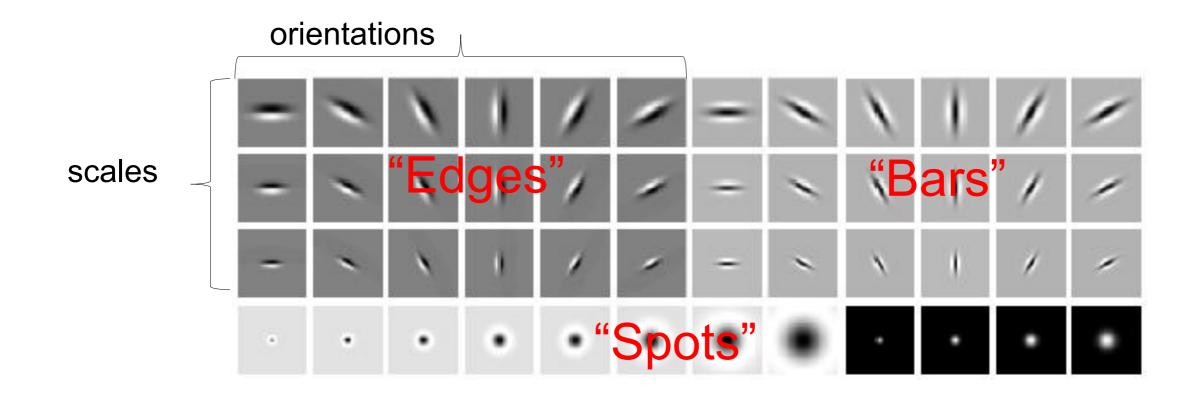
## What is texture?

Regular or stochastic patterns caused by bumps, grooves, and/or markings

## How can we represent texture?

 Compute responses of blobs and edges at various orientations and scales

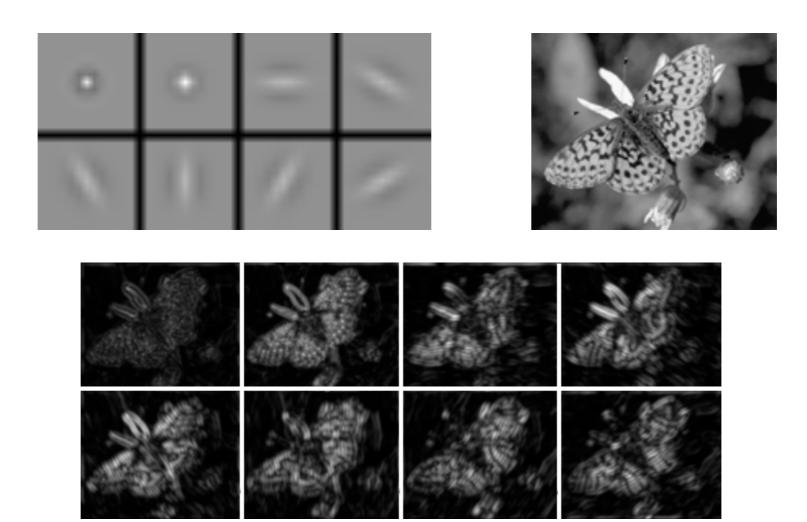
#### **Overcomplete representation: filter banks**



#### Code for filter banks: www.robots.ox.ac.uk/~vgg/research/texclass/filters.html

# Filter banks

Process image with each filter and keep responses (or squared/abs responses)

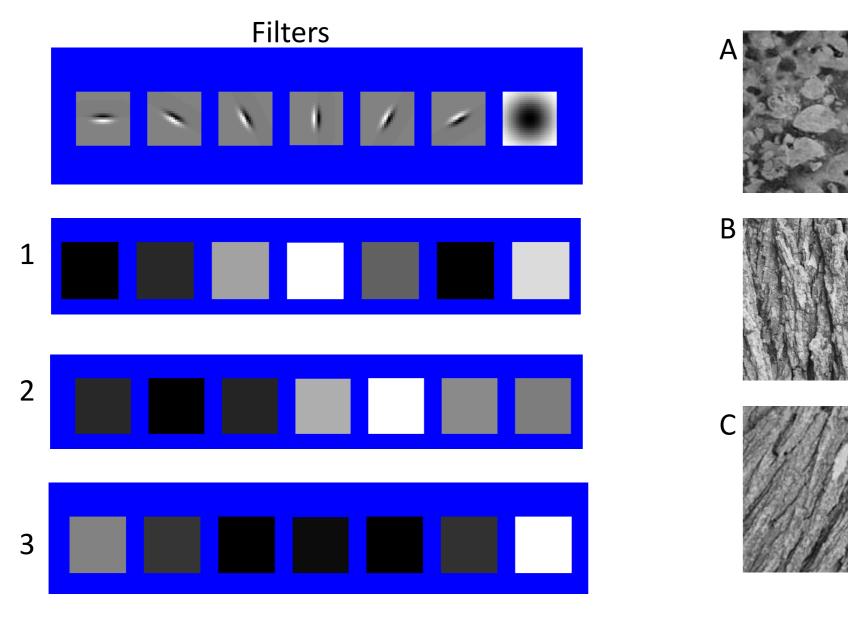


## How can we represent texture?

 Measure responses of blobs and edges at various orientations and scales

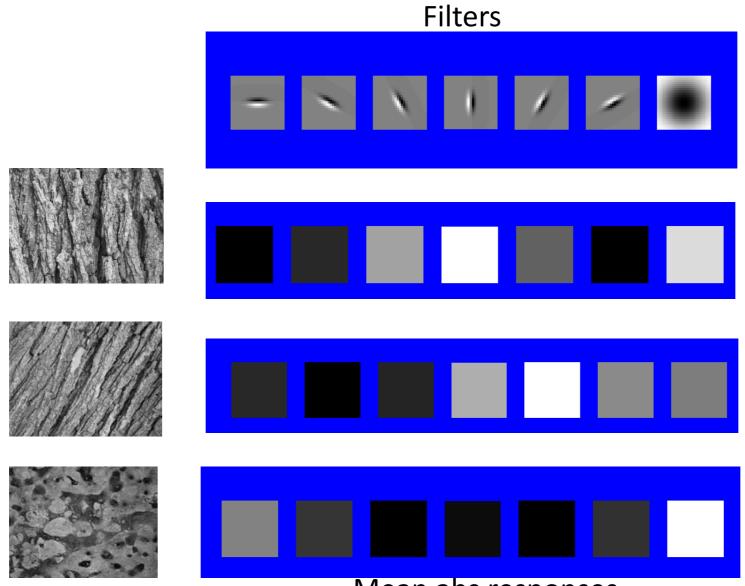
 Idea 1: Record simple statistics (e.g., mean, std.) of absolute filter responses

#### Can you match the texture to the response?



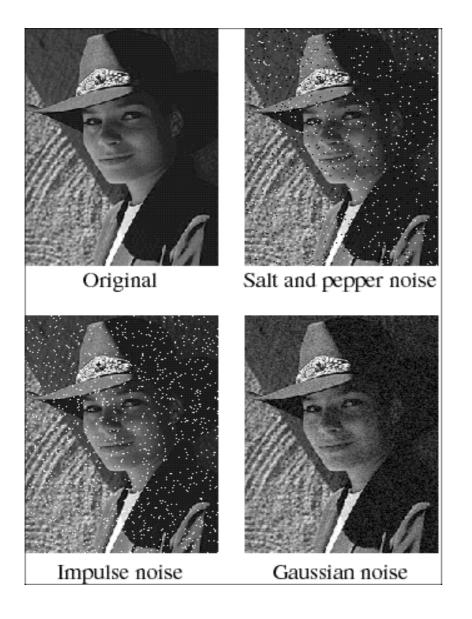
Mean abs responses

#### Representing texture by mean abs response



Mean abs responses

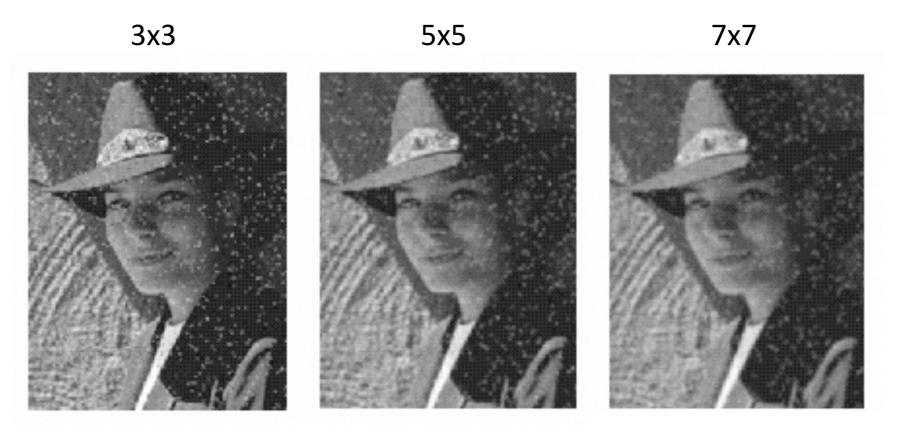
## **Denoising and Nonlinear Image Filtering**



- Salt and pepper noise: contains random occurrences of black and white pixels
- Impulse noise: contains random occurrences of white pixels
- Gaussian noise: variations in intensity drawn from a Gaussian normal distribution

Source: S. Seitz

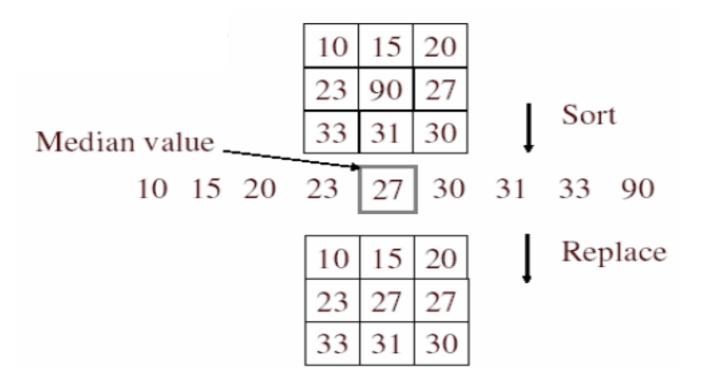
# Reducing salt-and-pepper noise



• What's wrong with the results?

# Alternative idea: Median filtering

• A median filter operates over a window by selecting the median intensity in the window



• Is median filtering linear?

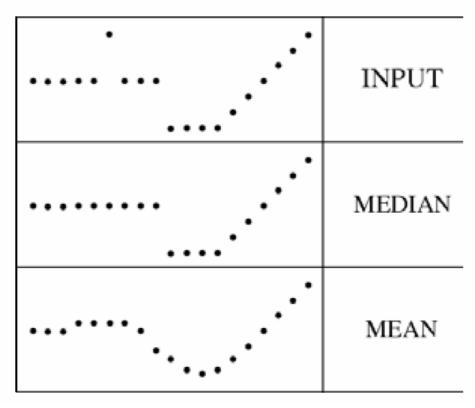
# Median filter

- Is median filtering linear?
- Let's try filtering

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 2 \\ 2 & 2 & 2 \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

# Median filter

- What advantage does median filtering have over Gaussian filtering?
  - Robustness to outliers

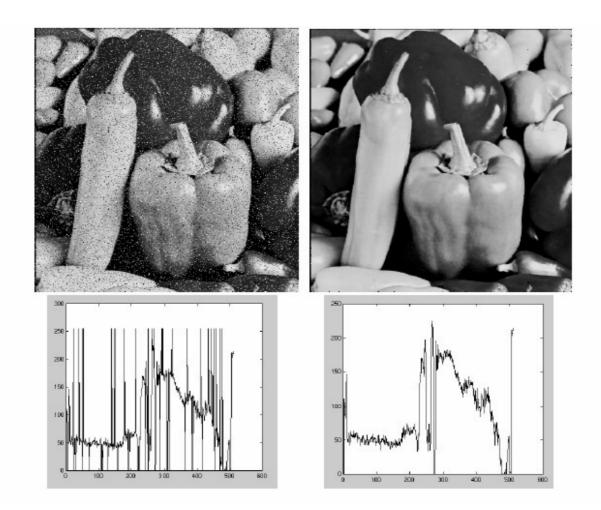


filters have width 5 :

Source: K. Grauman

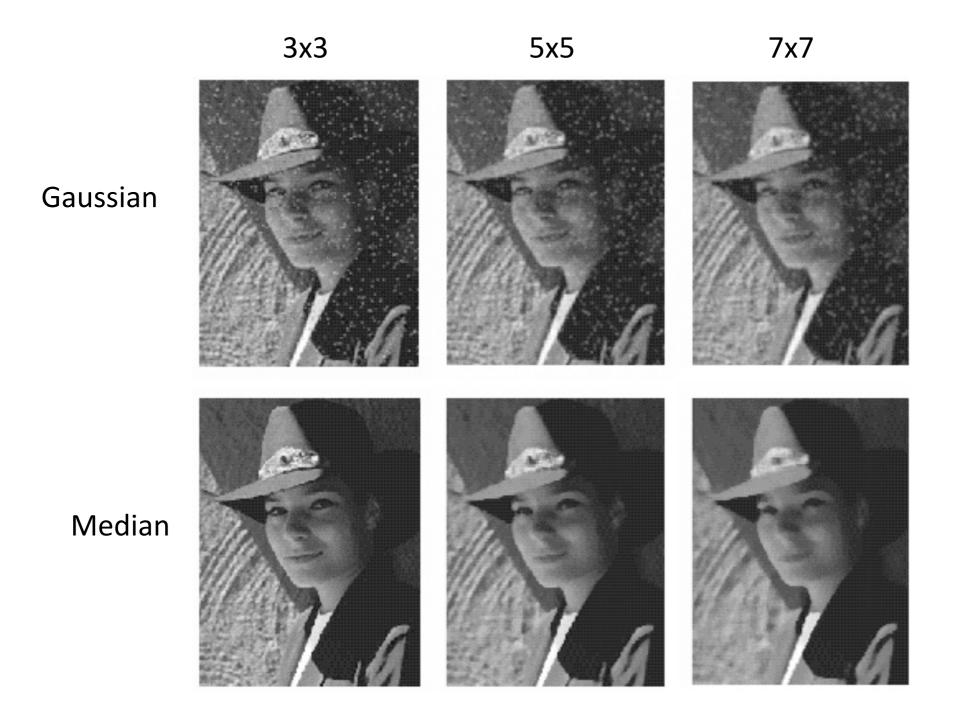
# Median filter

#### Salt-and-pepper Median noise filtered



MATLAB: medfilt2(image, [h w])

#### Gaussian vs. median filtering



# Other non-linear filters

- Weighted median (pixels further from center count less)
- Clipped mean (average, ignoring few brightest and darkest pixels)
- Bilateral filtering (weight by spatial distance and intensity difference)



**Bilateral filtering** 

# Things to remember

- Linear filtering is sum of dot product at each position
  - Can smooth, sharpen, translate (among many other uses)
- Gaussian filters
  - Low pass filters, separability, variance
- Attend to details:
  - filter size, extrapolation, cropping
- Application: representing textures
- Noise models and nonlinear image filters

